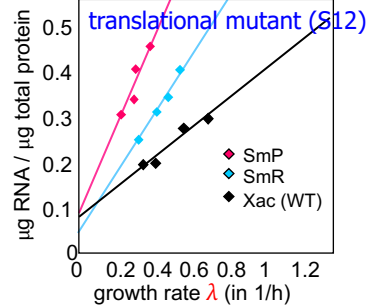
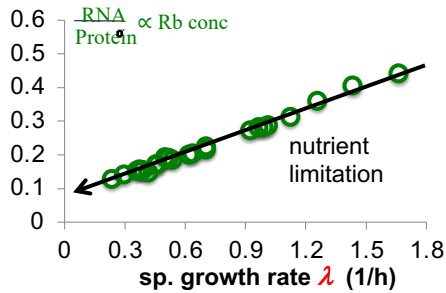


Microbial growth law [Ole Maaloe et al, 1950s - 70s]



Model of bacterial growth

- assume **all ribosomes efficiently engaged in protein synthesis**

rate protein mass accum. = rate Rb elongation

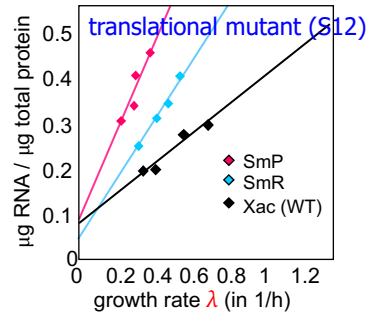
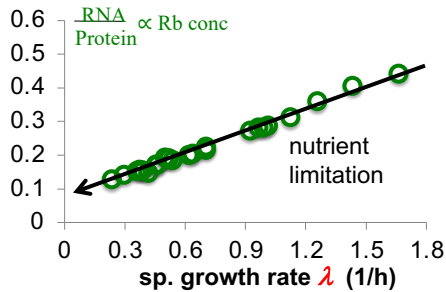
$$\dot{M}_{tot} = \lambda \cdot M_{tot} \quad \uparrow \quad \uparrow \quad \gamma \cdot M_{Rb}$$

$$\phi_R \equiv \frac{M_{Rb}}{M_{tot}} = \lambda / \gamma$$

λ : specific growth rate
 γ : Rb elongation rate
 (~20 aa/s or 10 Rb/hr)

1

Microbial growth law [Ole Maaloe et al, 1950s - 70s]

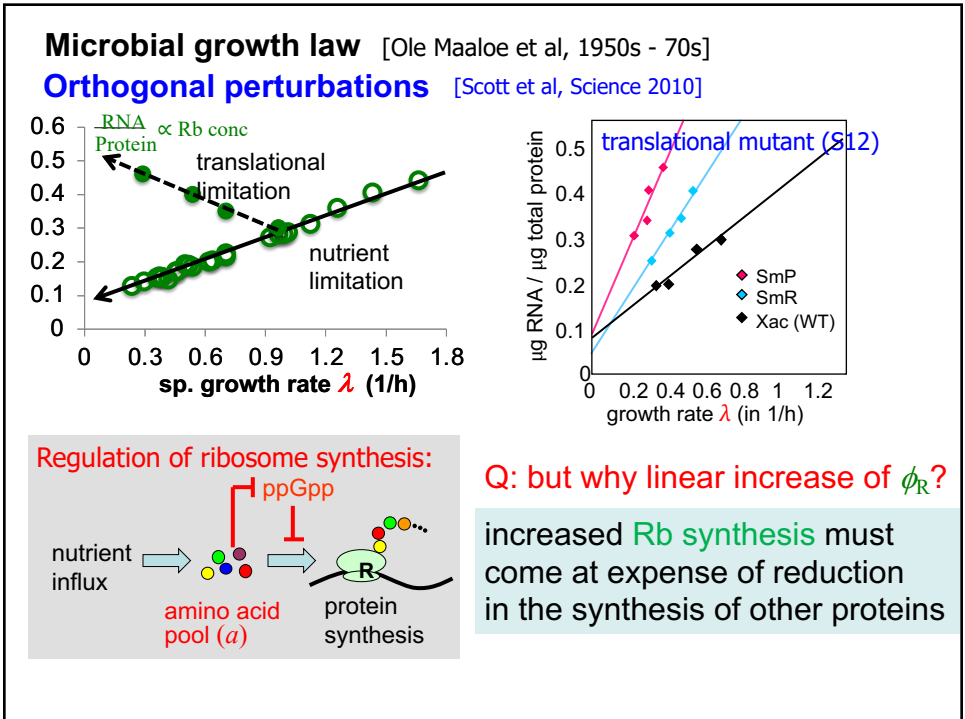


Model of bacterial growth

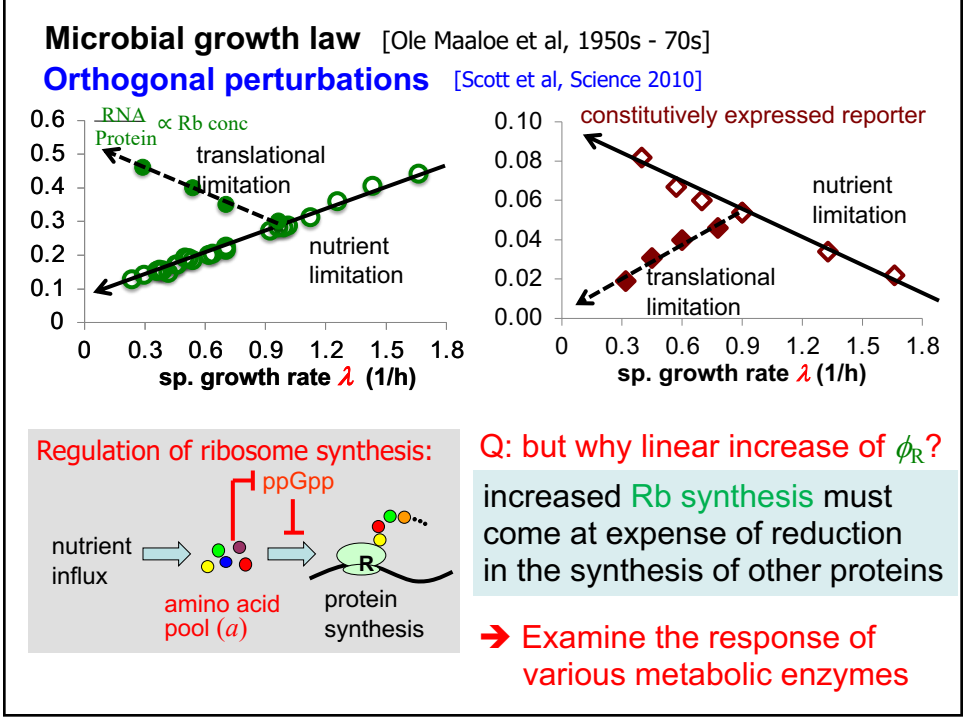
- assume **all ribosomes efficiently engaged in protein synthesis**

→ higher ribosomal content is required for fast growth
 → protein expressions are globally coupled if most ribosomes are engaged in translation

2



3



4

Catabolite repression & carbon hierarchy

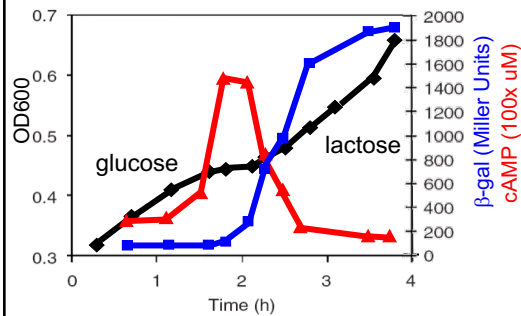
- glucose effect: ability of glucose to inhibit the synthesis of certain enzymes
- all glucose-sensitive enzymes can convert their substrates to metabolites which can also be obtained more readily by the metabolism of glucose

→ “catabolites” formed rapidly from glucose would accumulate and repress the formation of enzymes whose activity would augment the already large intracellular pools of these compounds

[B. Magasanik, 1961]

carbon hierarchy (e.g., glucose-lactose diauxie)

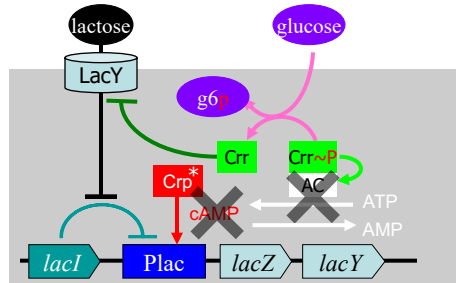
cAMP as a messenger (“inverse” of “catabolites”)



8

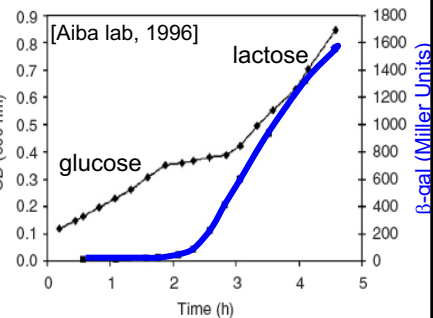
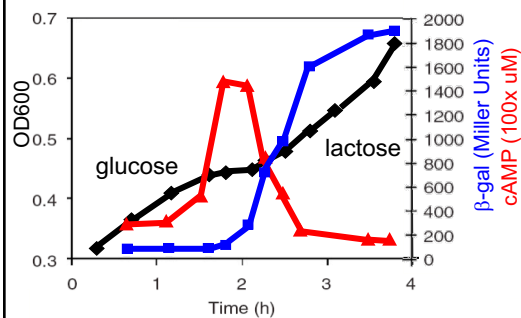
Catabolite repression & carbon hierarchy

Standard model



Problems with the standard model

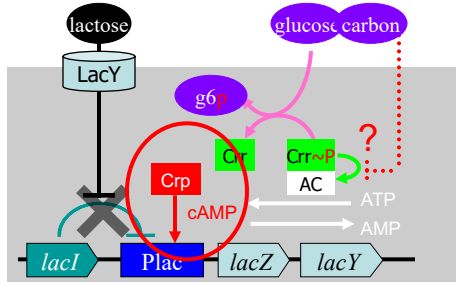
- diauxie does not require cAMP (mediated by “inducer exclusion”; later)



9

Catabolite repression

Standard model



Problems with the standard model

- diauxie does not require cAMP (mediated by "inducer exclusion"; later)
- effect not specific to glucose

- Q1: how is cAMP level controlled?
 Q2: what are the "catabolites"?
 Q3: physiological function?
 Q4: what about carbon hierarchy?

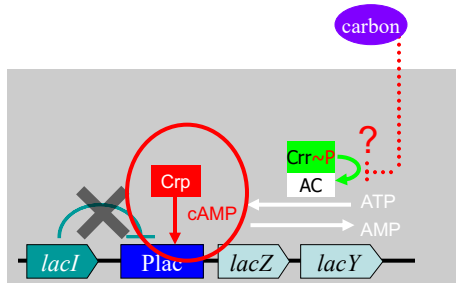
[J. Mandelstam, 1962]

Carbon source	β -Galactosidase (units/mg. dry wt.)	Doubling time (min.)
Lactose	136	45
Glucose	200	48
Gluconate	260	50
Galactose	432	54
Glycerol	499	60
Succinate	600	65
Fructose	613	67
Lactate	816	65

10

Catabolite repression

Standard model



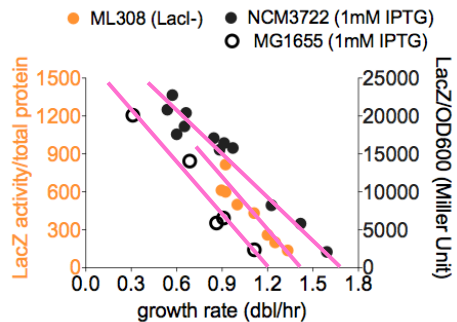
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- diauxie does not require cAMP (mediated by "inducer exclusion"; later)
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 Q3: physiological function?
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[J. Mandelstam, 1962]

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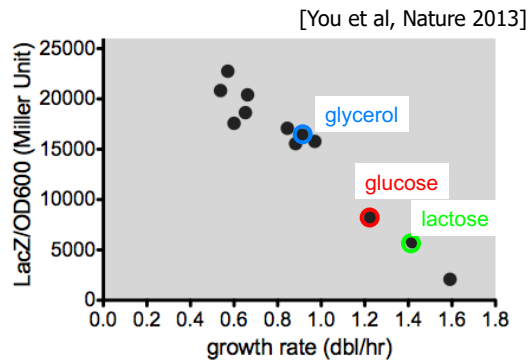


12

Physiological study of catabolite repression

E. coli K-12 NCM3722
(1mM IPTG)

C-source	dbl rate (dbl/h)	β-gal (Miller)
glucose6p + gluconate	1.59	2085
lactose	1.42	5803
glucose	1.22	8225
maltose	0.97	15789
glycerol	0.91	16431
pyruvate	0.88	15557
fructose	0.84	17080
succinate	0.66	20406
sorbitol	0.65	18636
mannose	0.60	17586
arabinose	0.57	22757
acetate	0.54	20834



13

Physiological study of catabolite repression

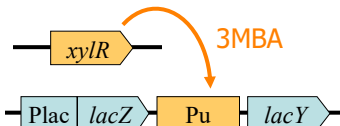
E. coli K-12 NCM3722
(1mM IPTG)

→ Up-regulation in response to reduced C-flux

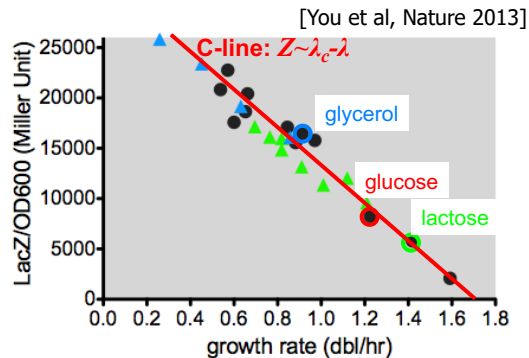
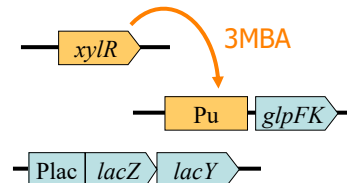
Q: what about other types of growth limitation?

no effect according to known regulation

titratable LacY expression



titratable GlpFK expression



▲ lactose with titratable LacY expression

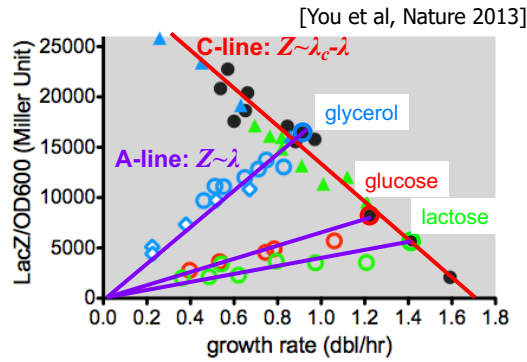
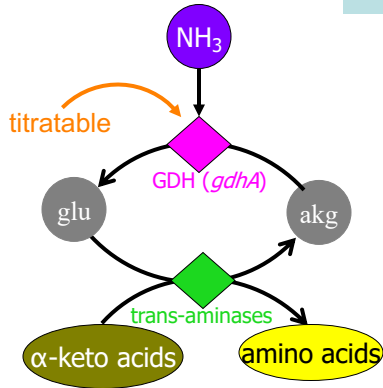
▲ glycerol with titratable GlpFK expression

14

Physiological study of catabolite repression

E. coli K-12 NCM3722
(1mM IPTG)

- Up-regulation in response to reduced C-flux
- Down-regulation of catabolism upon other nutrient limitations (A-lines)



[You et al, Nature 2013]

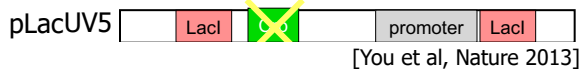
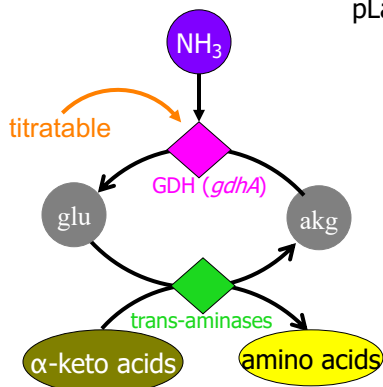
- ▲ lactose with titratable LacY expression
- ▲ glycerol with titratable GlpFK expression
- ○ ○ Δ gltD; titratable GDH; various C-sources
- ◇ S-limited chemostat; glycerol

17

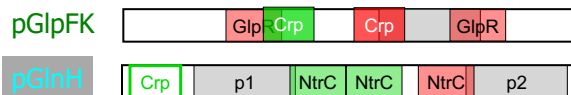
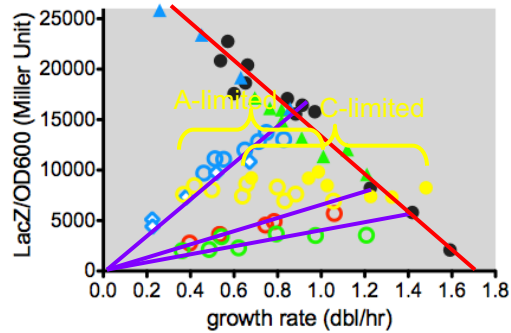
Physiological study of catabolite repression

E. coli K-12 NCM3722
(1mM IPTG)

- Dependence on Crp-cAMP?
- both C- and A- lines require Crp-cAMP



[You et al, Nature 2013]



18

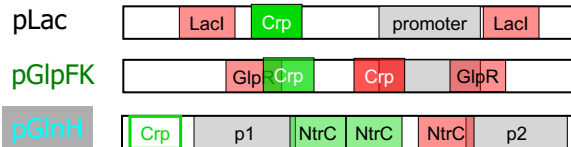
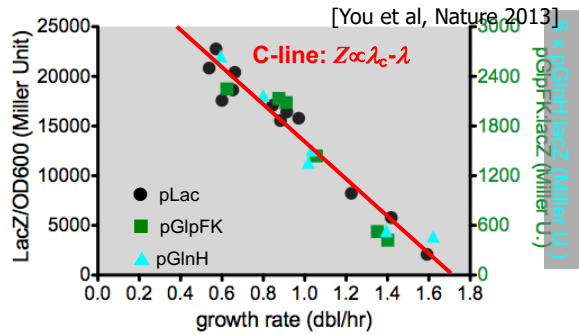
Physiological study of catabolite repression

Strain: NCM3722
(1mM IPTG)

C-source	dbl rate (dbl/h)	β -gal (Miller)
glucose6p+gluconate	1.59	2085
lactose	1.42	5803
glucose	1.22	8225
maltose	0.97	15789
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mannose	0.60	17586
arabinose	0.57	22757
acetate	0.54	20834

Dependence on Crp-cAMP?

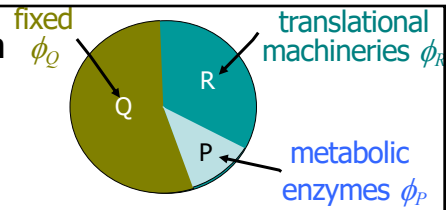
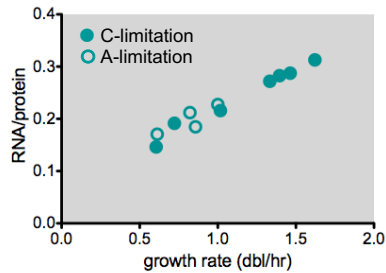
- both C- and A- lines require Crp-cAMP
- same C-line (λ_c) from different promoters



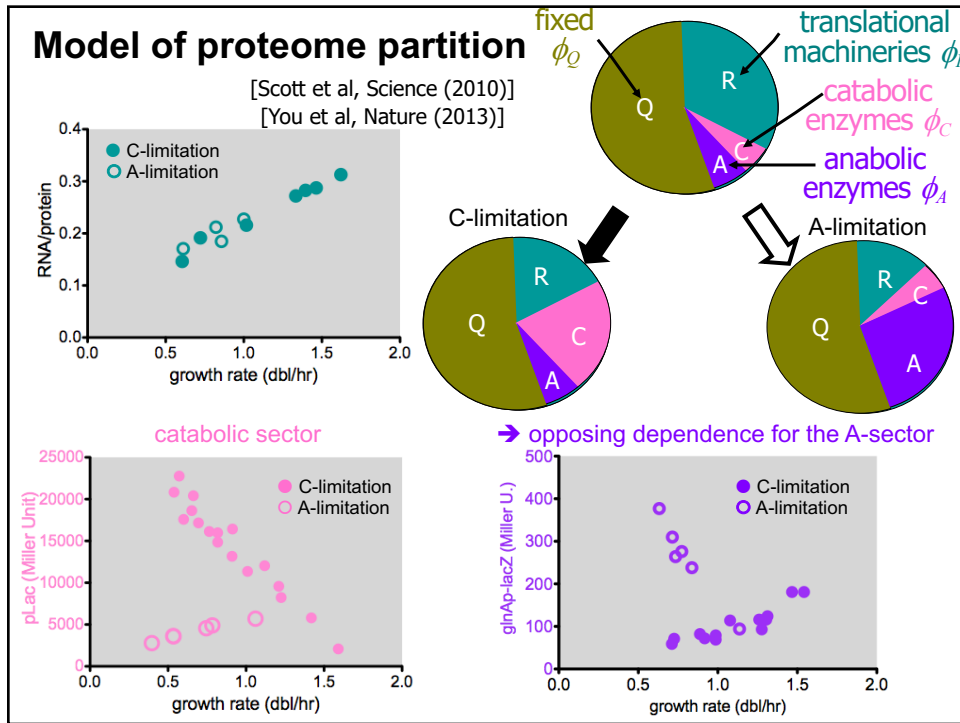
19

Model of proteome partition

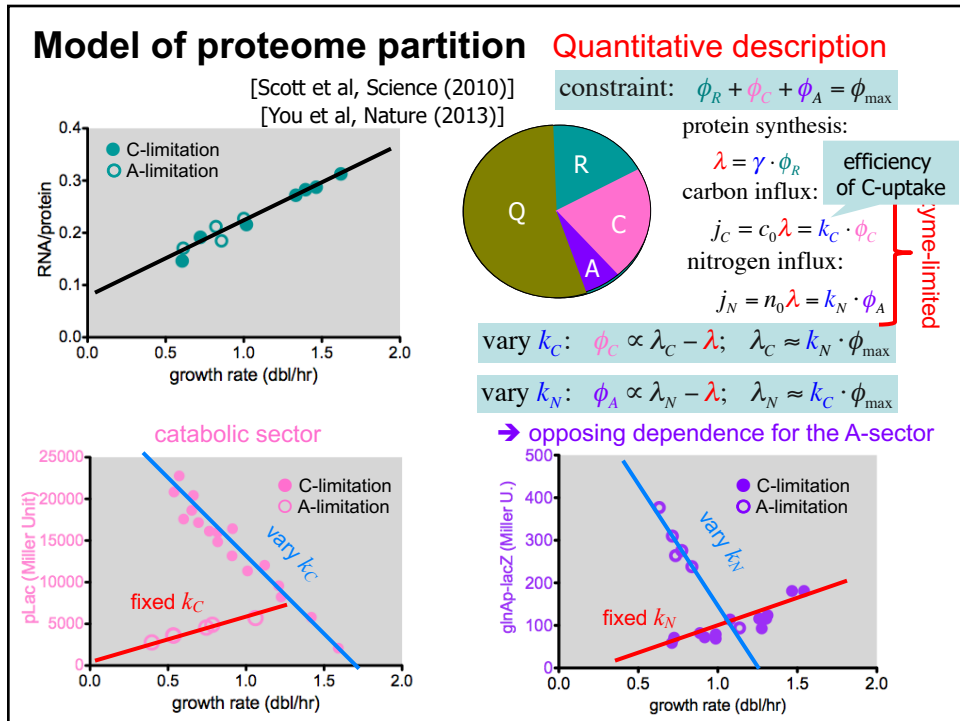
[Scott et al, Science (2010)]



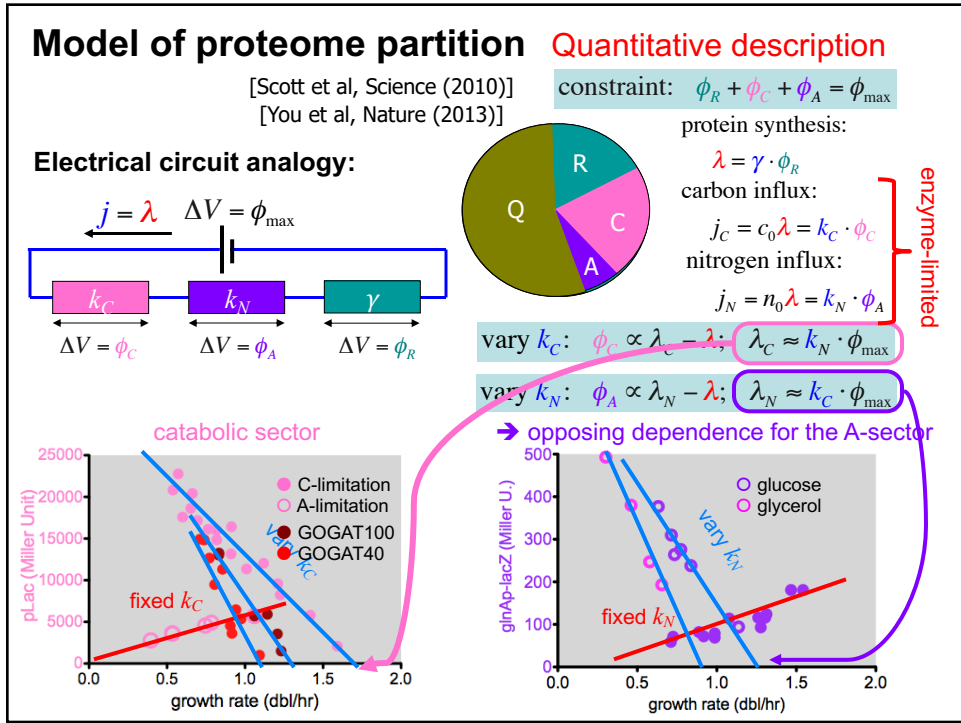
23



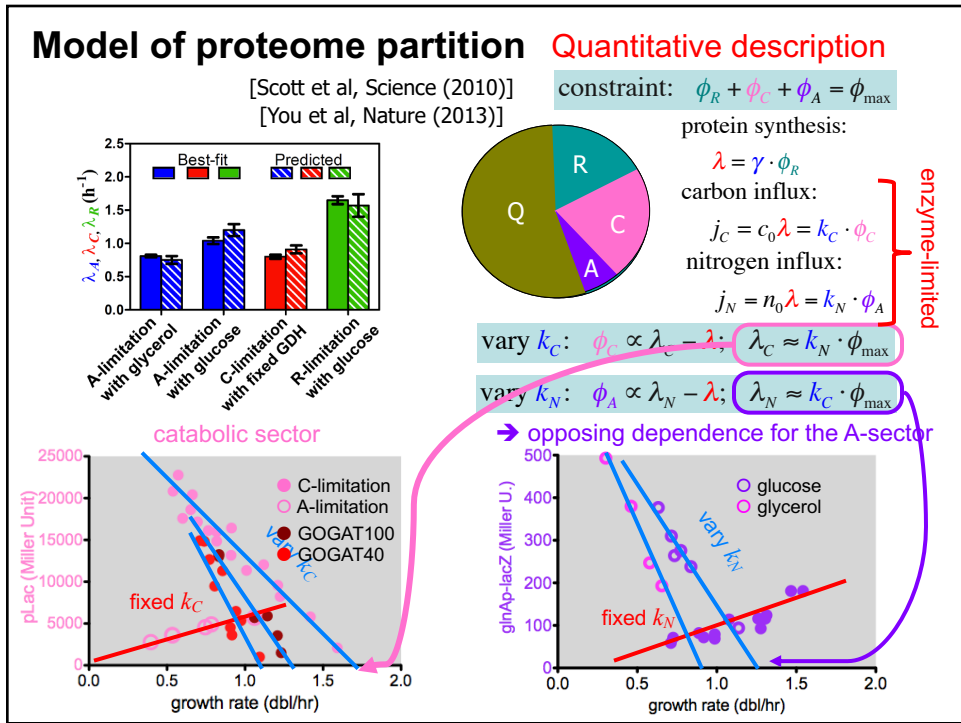
24



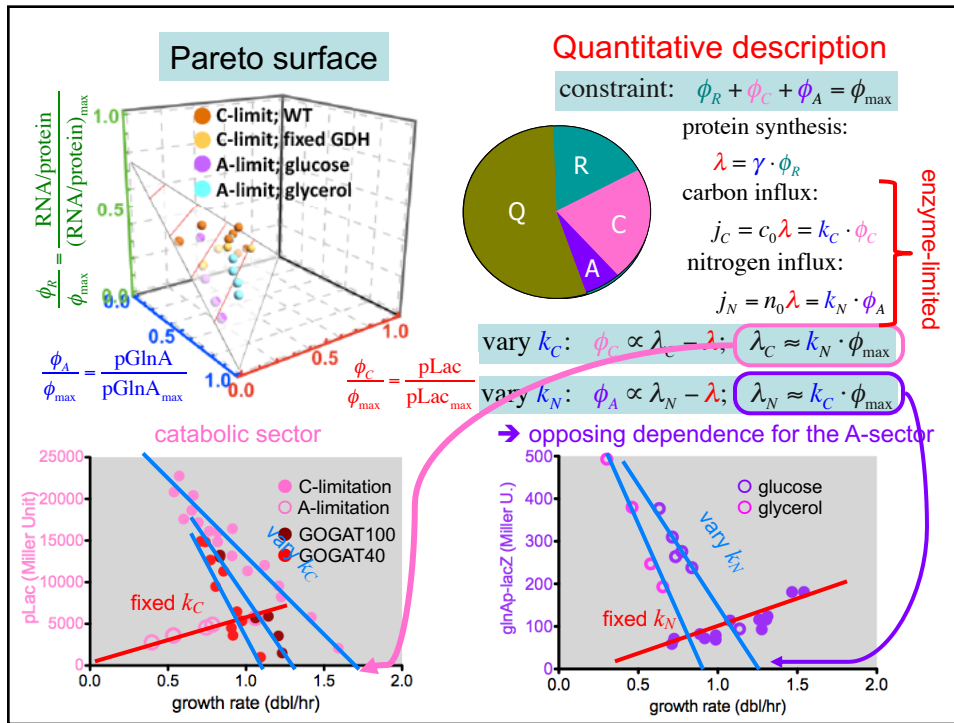
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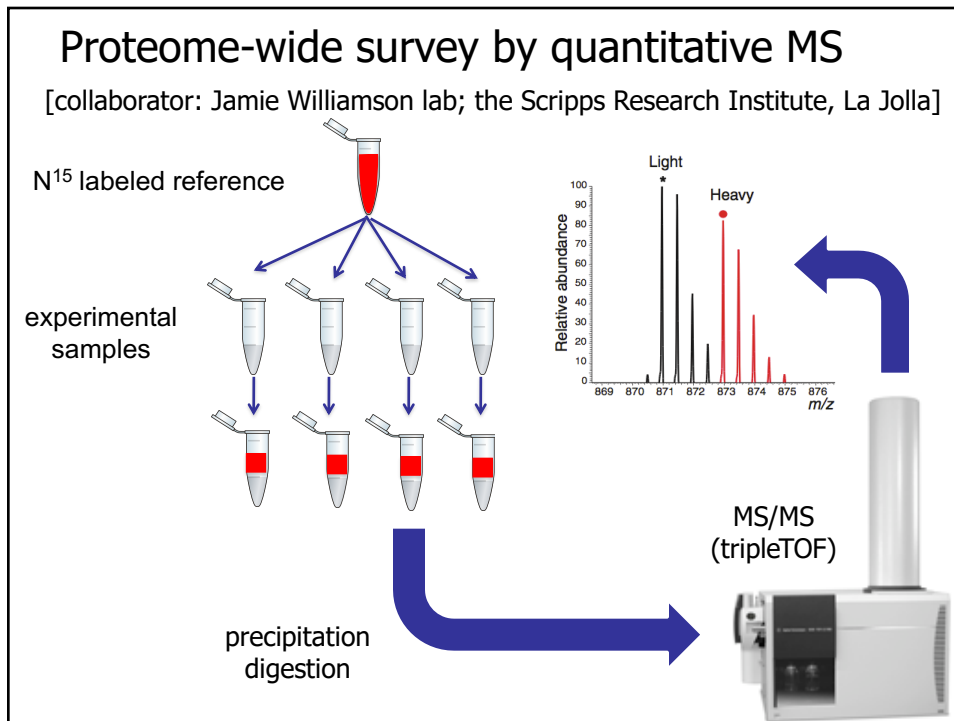
26



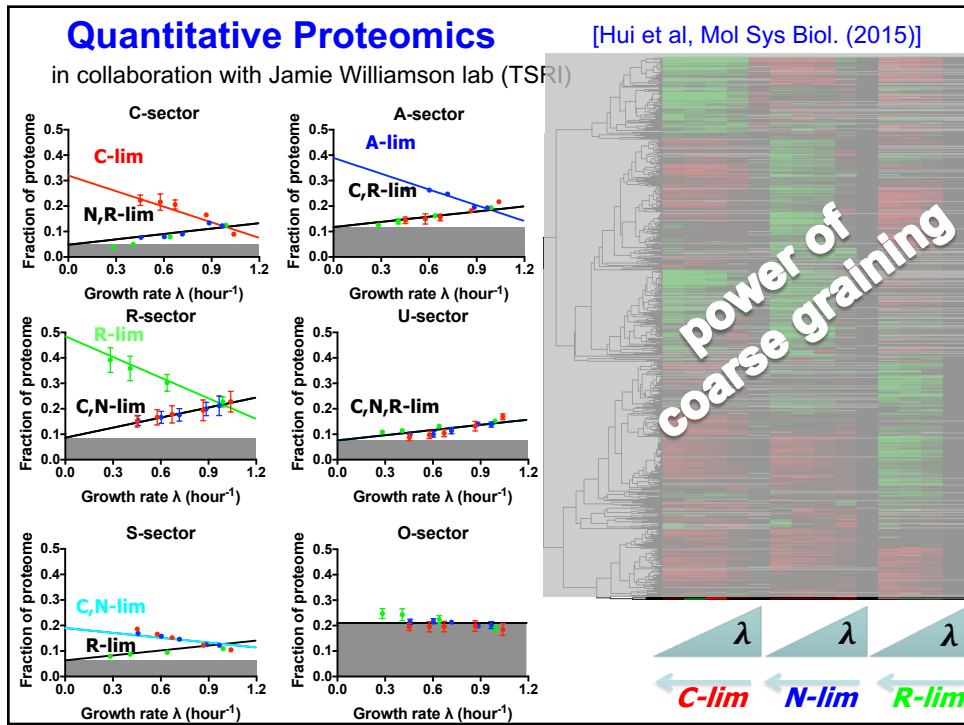
27



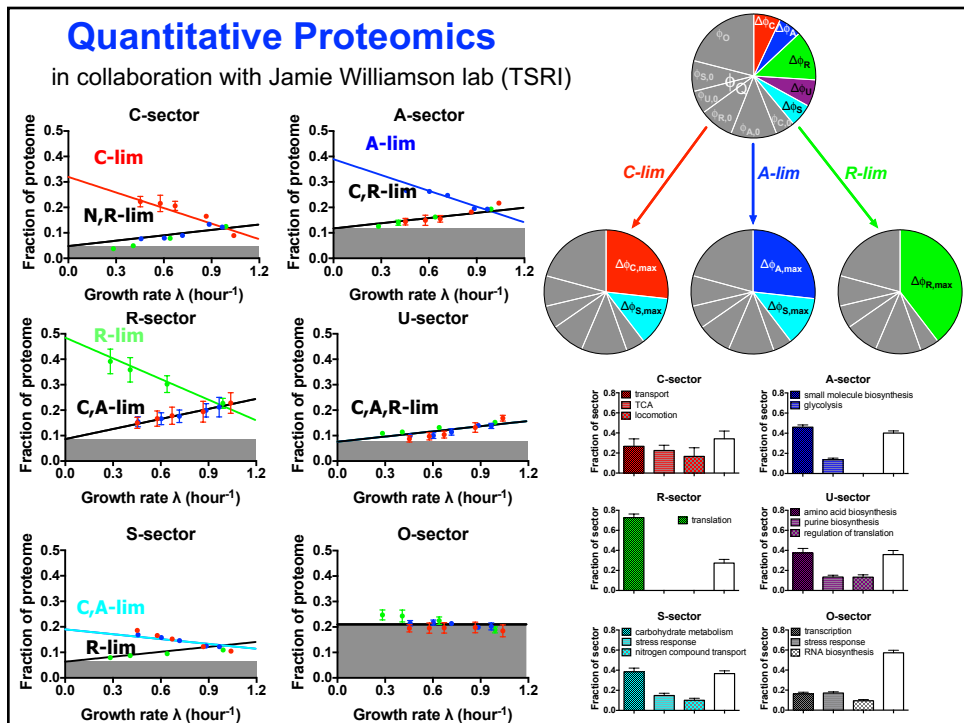
28



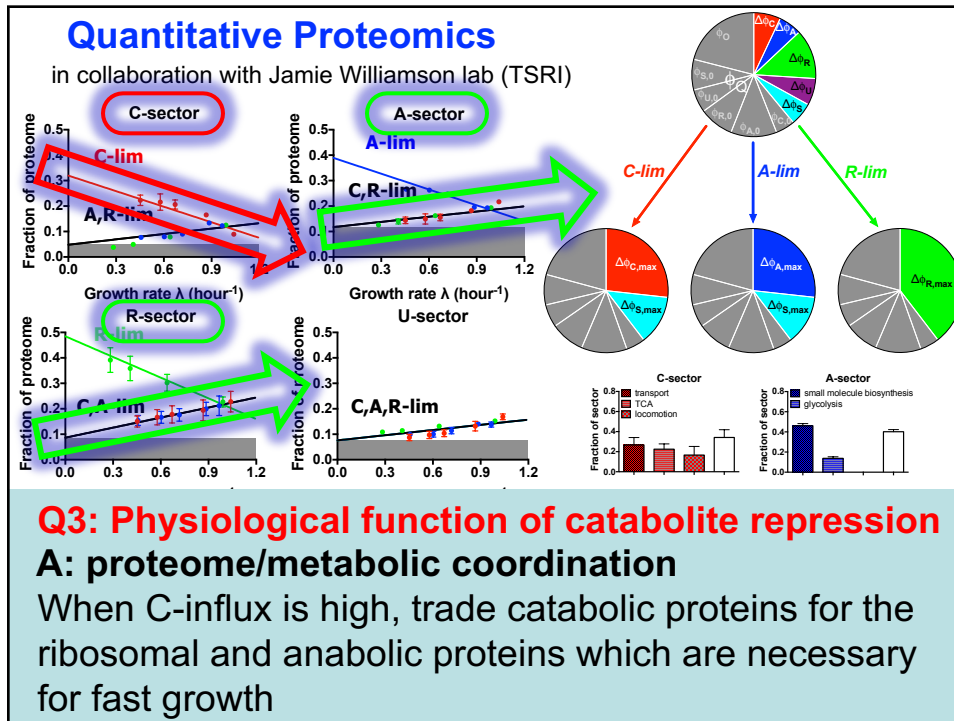
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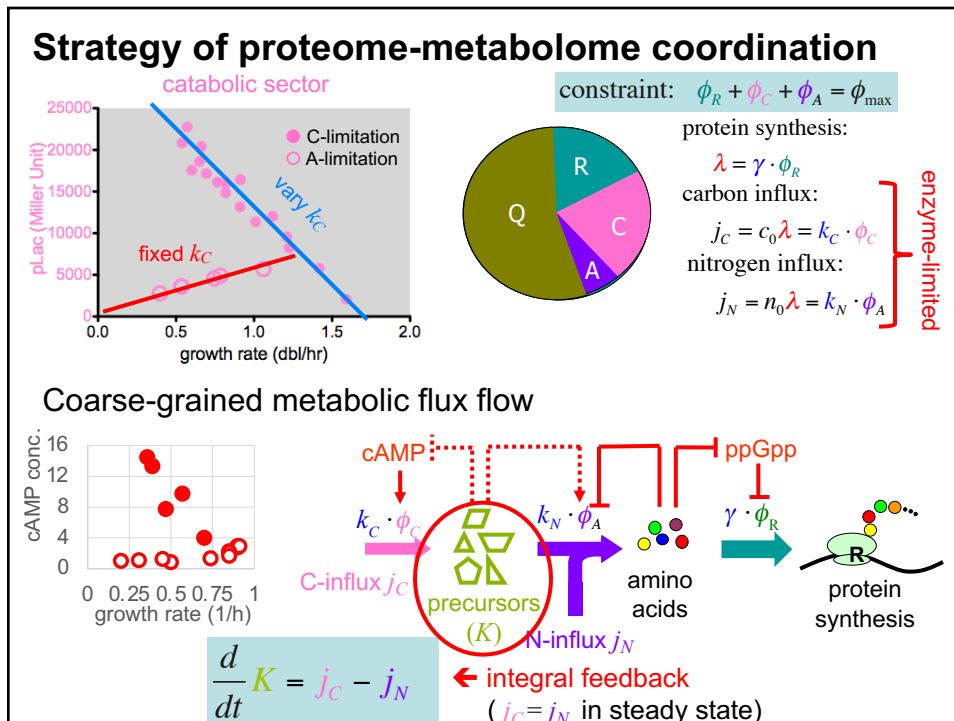
31



32



33

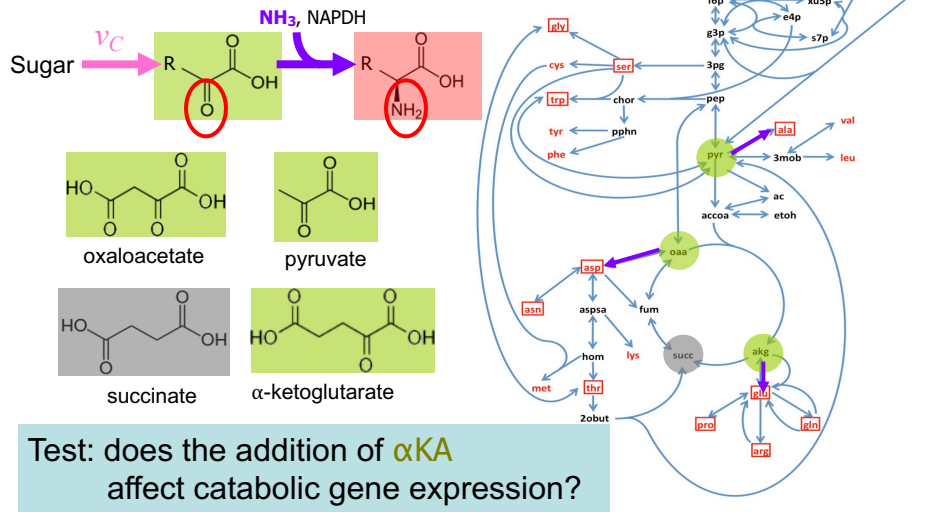


34

Strategy of proteome metabolic coordination

Simplest scenario: feedback by α -ketoacids (α KA)

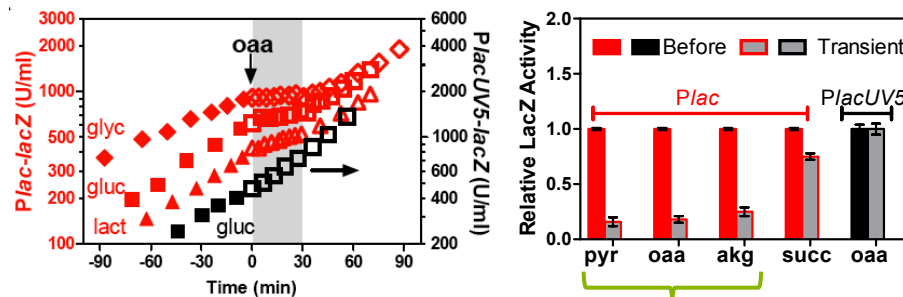
All amino acids synthesized from amination of α KAs



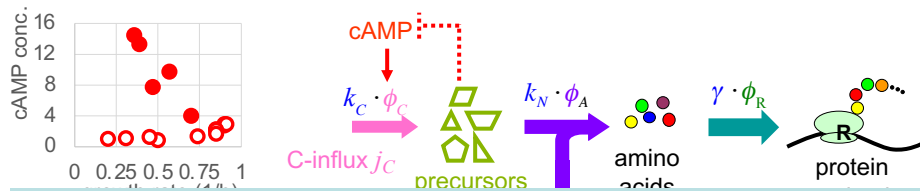
Test: does the addition of α KA affect catabolic gene expression?

35

Testing the carbon precursor feedback model



Coarse-grained metabolic flux flow



Q2: What are the "catabolites"?

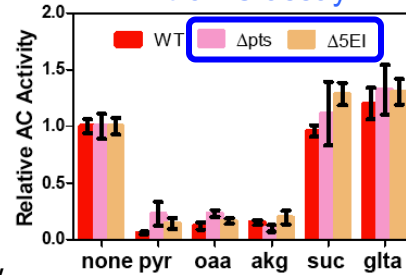
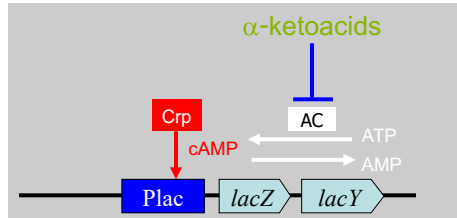
A: alpha ketoacids

36

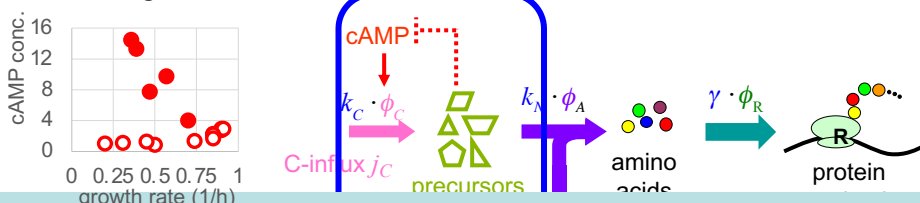
Testing the carbon precursor feedback model

mechanism? PTS not necessary

in vitro AC assay



Coarse-grained metabolic flux flow



Q1: How is cAMP level controlled?

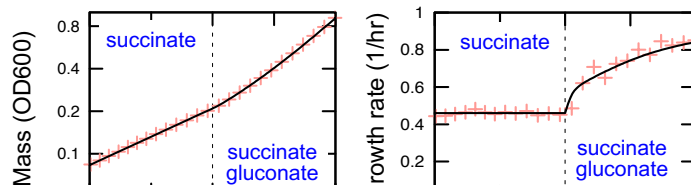
A: direct inhibition of AC activity by alpha ketoacids

40

Growth transition kinetics

[Erickson et al, Nature (2017)]

Nutrient upshift



Coarse-grained kinetic model requiring only

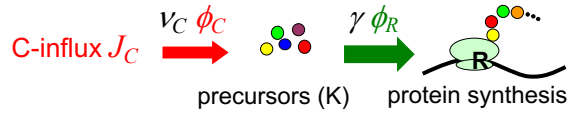
- single ordinary differential equation
- values of the initial and final growth rates (to define C quality)
- steady-state growth laws
- describes gene expression and growth curve throughout the course of the transition
- no need for kinetic parameters; no fitting parameter
- works both for nutrient upshifts and downshifts
- same theory describes growth inhibition by antibiotics

41

Growth transition kinetics

[Erickson et al, Nature (2017)]

coarse-grained
metabolism

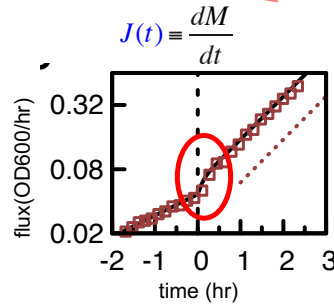
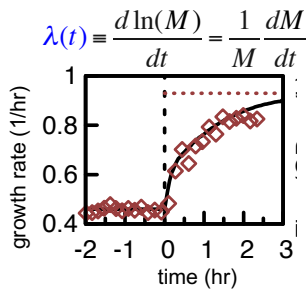


steady-state growth laws

$$\left\{ \begin{array}{l} \text{protein synthesis: } \lambda = \gamma \cdot \phi_R \\ \text{carbon uptake: } \lambda = v_C \cdot \phi_C \end{array} \right.$$

adiabatic approximation:

~~$$\frac{d\lambda}{dt} = \lambda(t) \cdot [v_C \phi_C(\lambda) - \lambda(t)]$$~~



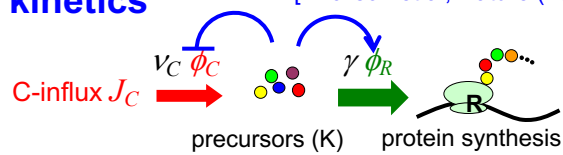
→ fast underlying kinetics manifested by biomass flux

42

Growth transition kinetics

[Erickson et al, Nature (2017)]

coarse-grained
metabolism



steady-state growth laws

$$\left\{ \begin{array}{l} \text{protein synthesis: } \lambda = \gamma \cdot \phi_R \\ \text{carbon uptake: } \lambda = v_C \cdot \phi_C \end{array} \right.$$

adiabatic approximation:

~~$$\frac{d\lambda}{dt} = \lambda(t) \cdot [v_C \phi_C(\lambda) - \lambda(t)]$$~~

fast kinetics: regulation by precursors (K)

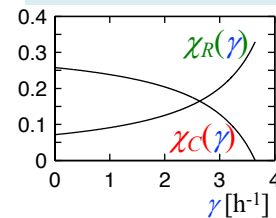
$$\frac{dK}{dt} = K(t) \cdot [v_C \chi_C(K) - \gamma(K) \chi_R(K)]$$

... but requires MANY molecular parameters

→ capture fast kinetics by following $\gamma(K(t))$

$$\frac{d\gamma}{dt} = \gamma \cdot [v_C \chi_C(\gamma) - \chi_R(\gamma)]$$

regulatory functions
from growth laws



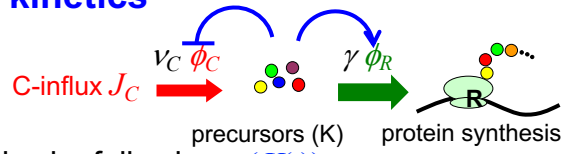
→ take reg functions $\chi_i(\gamma)$ as given by steady state: $\chi_i(\gamma(\lambda)) = \phi_i(\lambda)$

44

Growth transition kinetics

[Erickson et al, Nature (2017)]

coarse-grained
metabolism

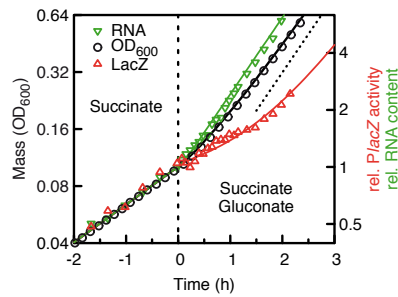


→ capture fast kinetics by following $\gamma(K(t))$

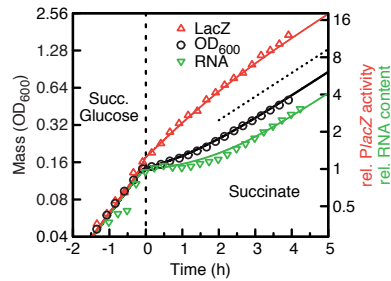
$$\frac{d\gamma}{dt} = \gamma \cdot [v_C \chi_C(\gamma) - \chi_R(\gamma)] \rightarrow M(t), M_R(t), M_C(t)$$

- exact solution; completely determined by λ_i, λ_f

nutrient upshift



nutrient downshift

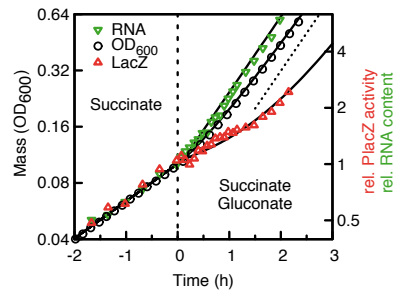
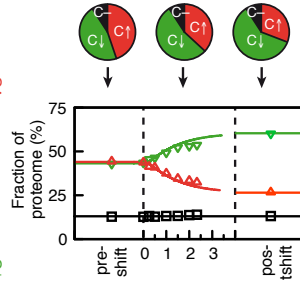
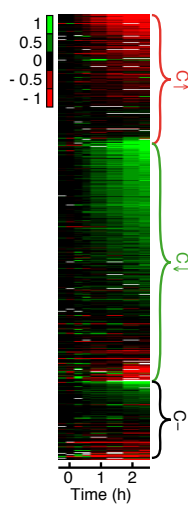


45

Growth transition kinetics

[Erickson et al, Nature (2017)]

proteome-wide response to nutrient up-shift



upshift kinetics:

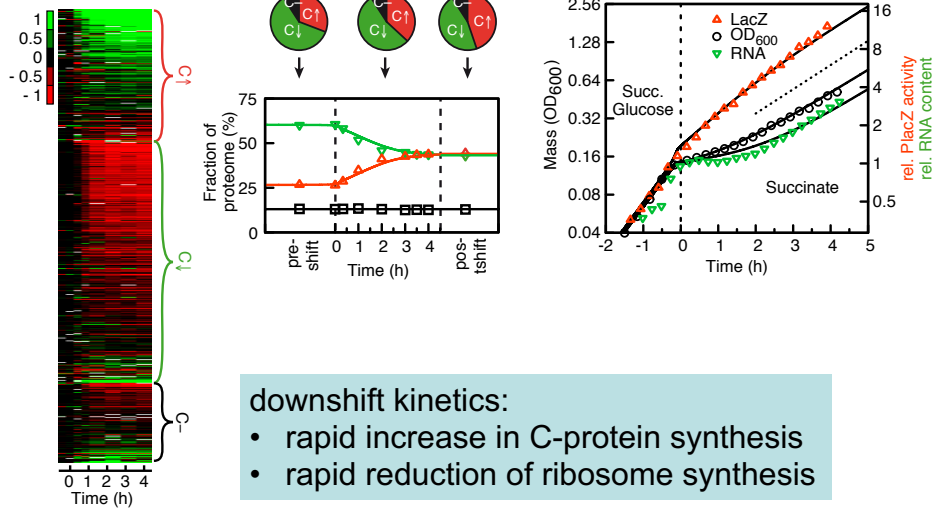
- rapid increase in ribosome synthesis
- rapid reduction of C-protein synthesis
- slow recovery of growth rate due to slow dilution of pre-existing C-proteins

46

Growth transition kinetics

[Erickson et al, Nature (2017)]

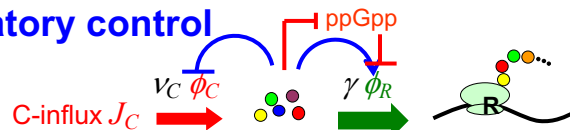
proteome-wide response to nutrient down-shift



47

Strategy of regulatory control

coarse-grained metabolism



fast kinetics: regulation by precursors (K)

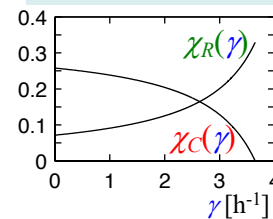
$$\frac{dK}{dt} = K(t) \cdot [v_C \chi_C(K) - \gamma(K) \chi_R(K)]$$

... but requires MANY molecular parameters

→ capture fast kinetics by following $\gamma(K(t))$

$$\frac{d\gamma}{dt} = \gamma \cdot [v_C \chi_C(\gamma) - \chi_R(\gamma)]$$

regulatory functions from growth laws



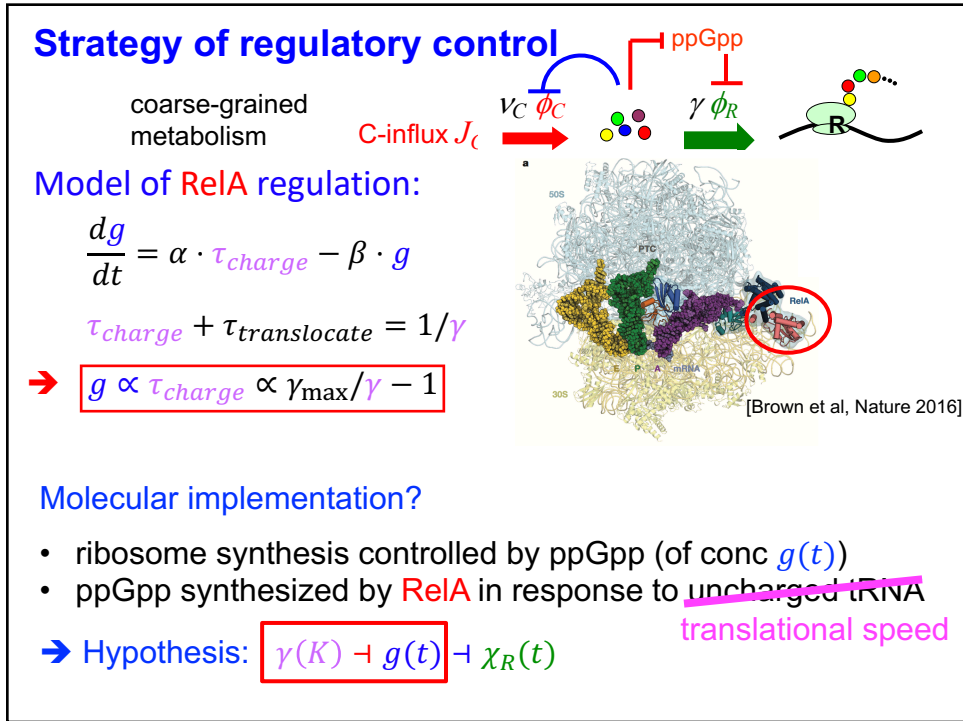
Molecular implementation?

- ribosome synthesis controlled by ppGpp (of conc $g(t)$)
- ppGpp synthesized by RelA in response to ~~uncharged tRNA~~

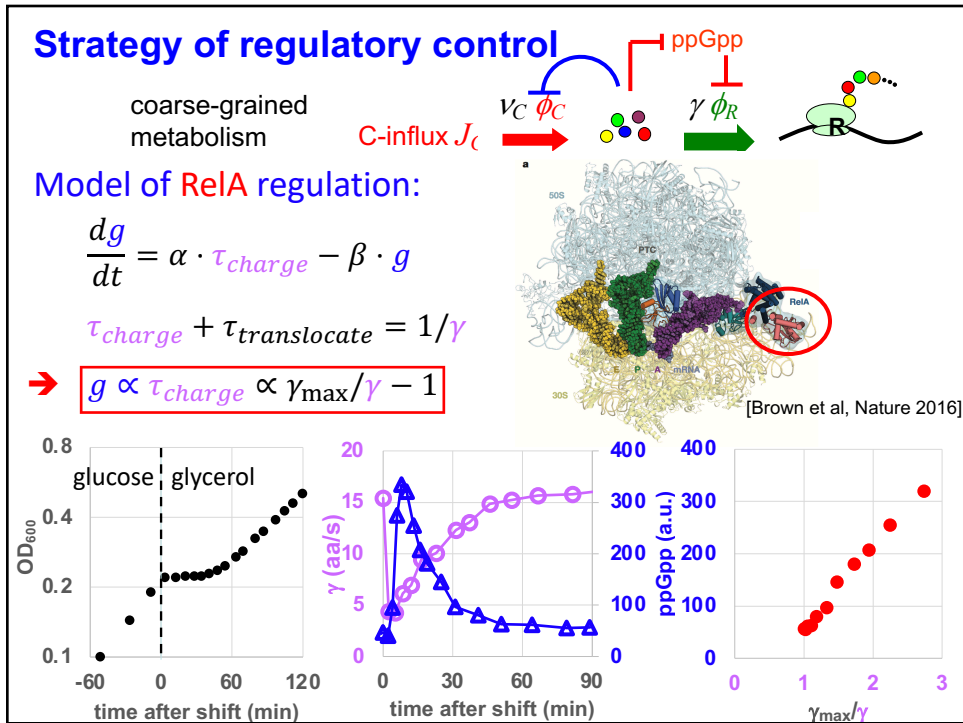
→ Hypothesis: $\gamma(K) \rightarrow g(t) \rightarrow \chi_R(t)$

translational speed

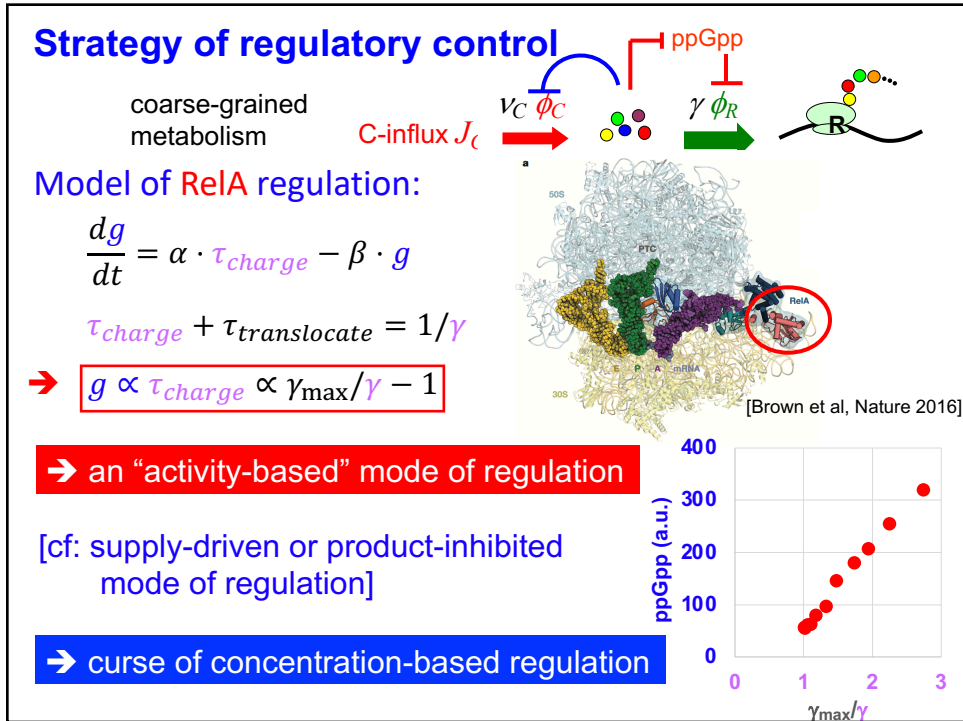
55



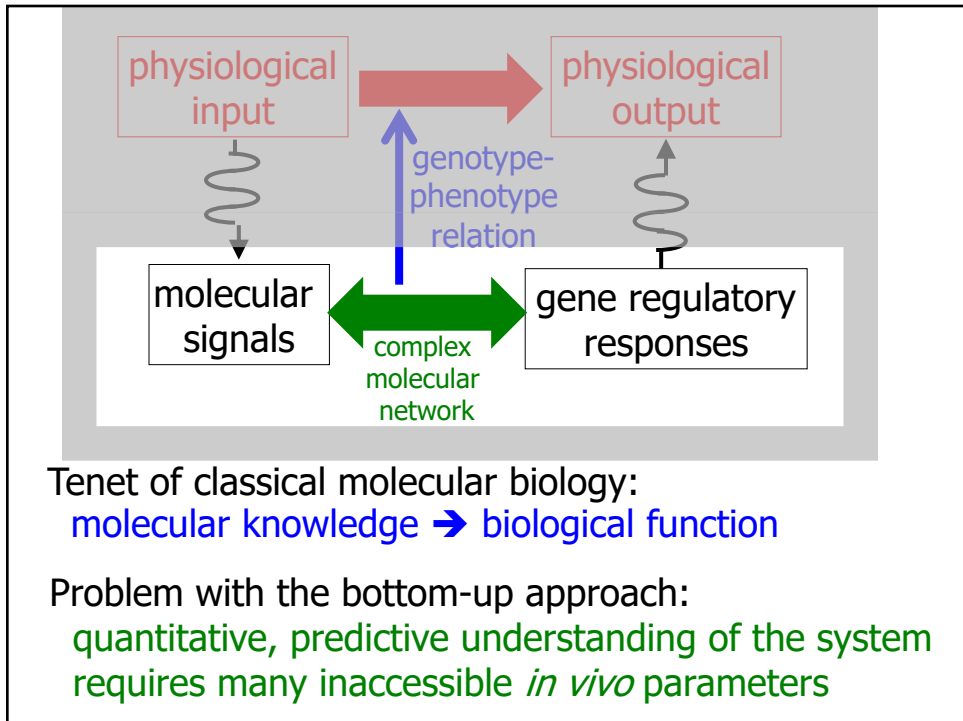
56



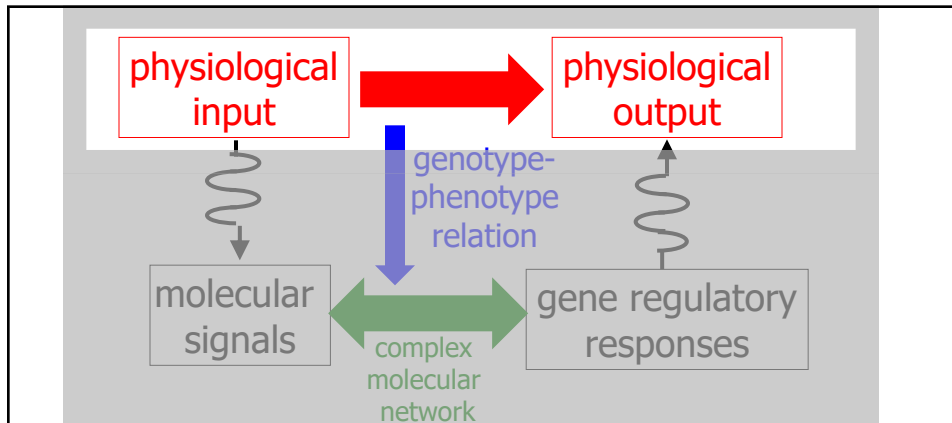
57



58



61

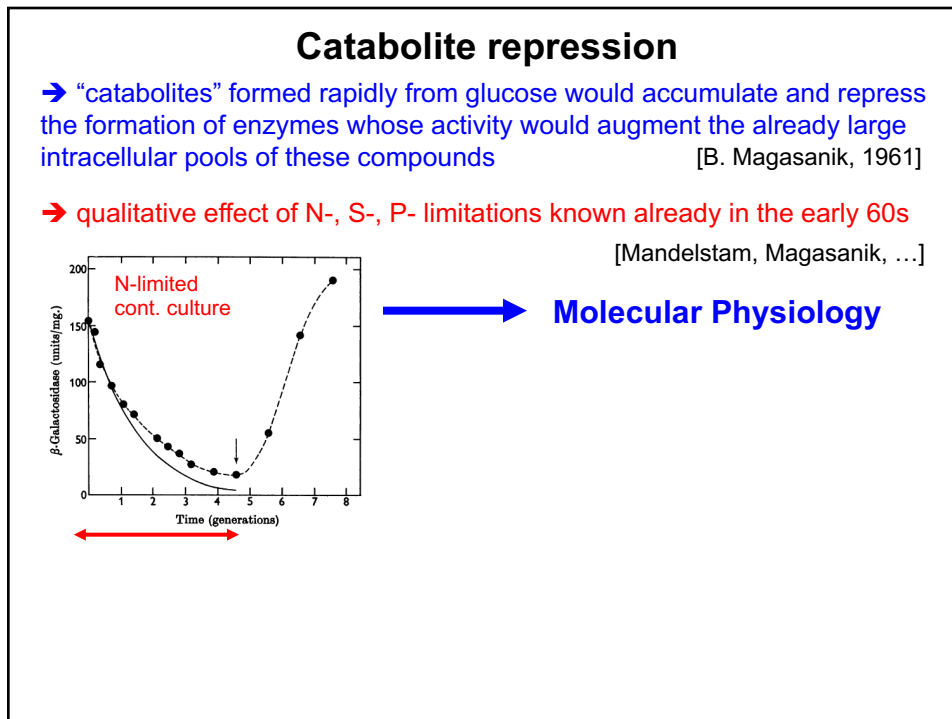


Top-down solution:

tame complexity by quantitative phenomenology ('laws')
 = simple relations between physiological inputs/outputs

- quantitative predictions on physiological responses
- useful guide for synthetic biology
- insight on the "purpose" of regulatory mechanisms
- guide for regulatory strategies & molecular implementations

62



63

Catabolite modulator factor: A possible mediator of catabolite repression in bacteria

(physiological repression and derepression/ β -galactosidase/adenosine 3':5'-cyclic monophosphate)

AGNES ULLMANN, FRANCOISE TILLIER, AND JACQUES MONOD*

ABSTRACT Water soluble extracts of *Escherichia coli* cells have been found to exert an extremely strong repressive effect upon the expression of catabolite sensitive operons. The compound responsible for this activity has been partially purified and proves to be of low molecular weight and heat stable. The effect of this compound, hereafter designated as catabolite modulator factor, is only partially antagonized by adenosine 3':5'-cyclic monophosphate. The possible role of catabolite modulator factor in the physiological regulation of catabolite repression is discussed.



Citing Articles

Author(s): KOLB, A; BUSBY, S; BUC, H; GARGES, S; ADHYA, S

Title: TRANSCRIPTIONAL REGULATION BY CAMP AND ITS RECEPTOR PROTEIN

Source: ANNUAL REVIEW OF BIOCHEMISTRY, 62: 749-795 1993

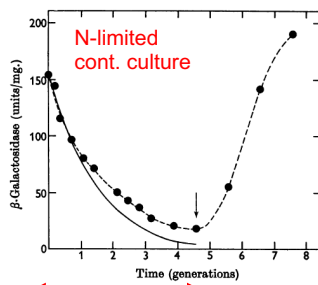
64

Catabolite repression

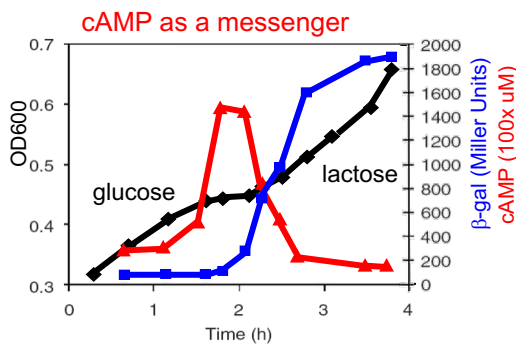
→ "catabolites" formed rapidly from glucose would accumulate and repress the formation of enzymes whose activity would augment the already large intracellular pools of these compounds [B. Magasanik, 1961]

→ qualitative effect of N-, S-, P- limitations known already in the early 60s

[Mandelstam, Magasanik, ...]



Molecular Physiology

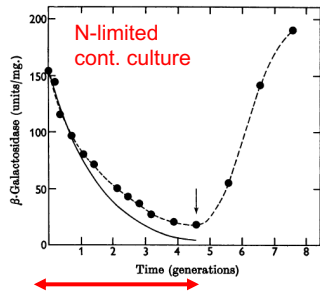


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Catabolite repression

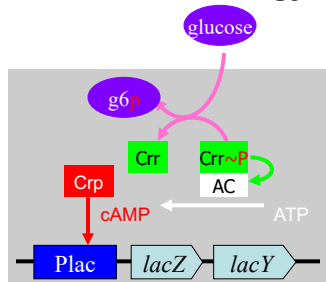
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→ **Molecular Physiology**

Molecular Zoology

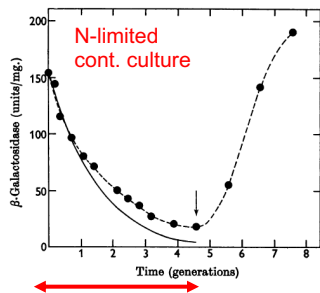


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Catabolite repression

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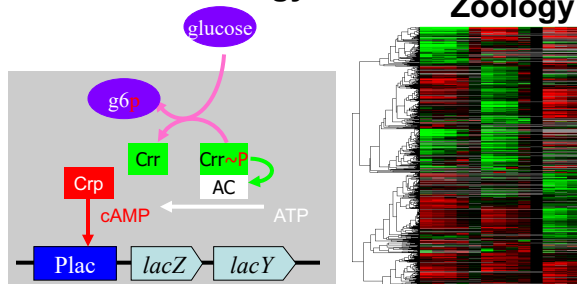
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→ **Molecular Physiology**

Molecular Zoology

Systems Zoology

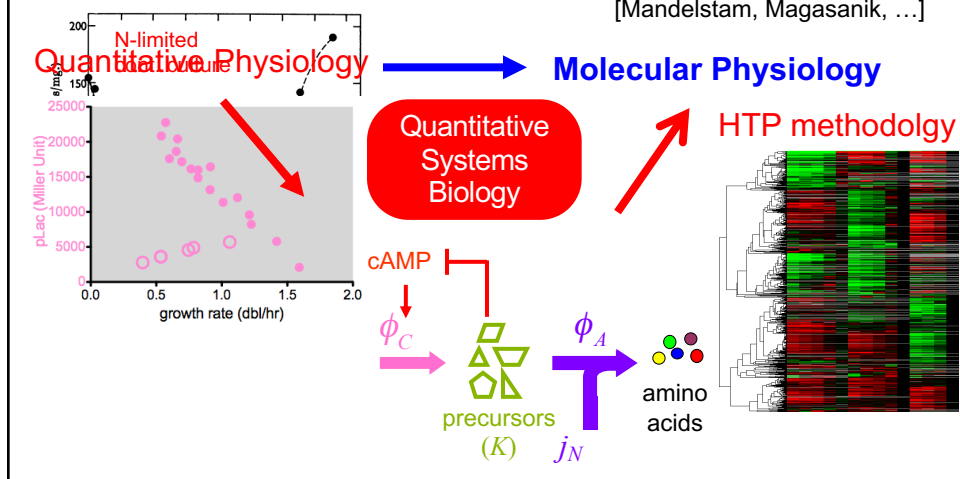


67

Catabolite repression

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68