

E. Quantitative characterization of the *lac* promoter

lac promoter of *E. coli*:

- best-studied system of molecular biology
 - all molecular components characterized
 - many mutants studied *in vivo*
 - most parameters measured *in vitro*
- exemplary model system of combinatorial gene regulation
 - involves activation, repression, and DNA looping

Quantitative confrontation of model and experiment

- applicability of the thermodynamic description of tsx control?
- can the *in vivo* behavior of a system be understood in terms of its molecular parts?

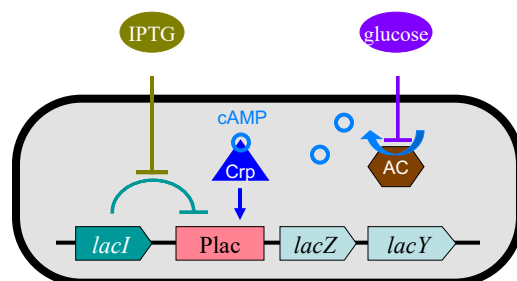
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Review: regulation of the *lac*-operon of *E. coli*

Physiology:

- *lac*-operon: utilization of lactose
- repressed by the **Lac Repressor** (encoded by *lacI*)
- repression alleviated by allo-lactose (by-product of lactose metabolism) or the synthetic inducer **IPTG**
- activated by the global regulator **Crp**; requires the inducer **cAMP**
- cAMP synthesized endogenously by **Adenylate Cyclase** (encoded by *cyaA*)
- activity of **AC** repressed by **glucose** uptake

Function: expression **ONLY** in the presence of lactose **AND** absence of glucose



qualitative behavior:

IPTG	glucose	expression
low	high	OFF
low	low	OFF
high	high	OFF
high	low	ON

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molecular ingredients:

- specific protein-DNA binding
- protein-protein interaction
- protein-mediated DNA looping

→ theory: quantitative prediction of gene regulation by LacI, cAMP-Crp

→ expt: characterize **LacZ** activity for different levels of regulatory proteins

-- control protein levels by varying the inducers (IPTG and cAMP)

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Quantitative characterization

Plac:gfp on plasmid

Previous expt: [Setty et al, PNAS, 2003]

Grow cells in medium with glucose, cAMP, IPTG

- use glucose to suppress cAMP synthesis
- control cAMP-level extracellularly

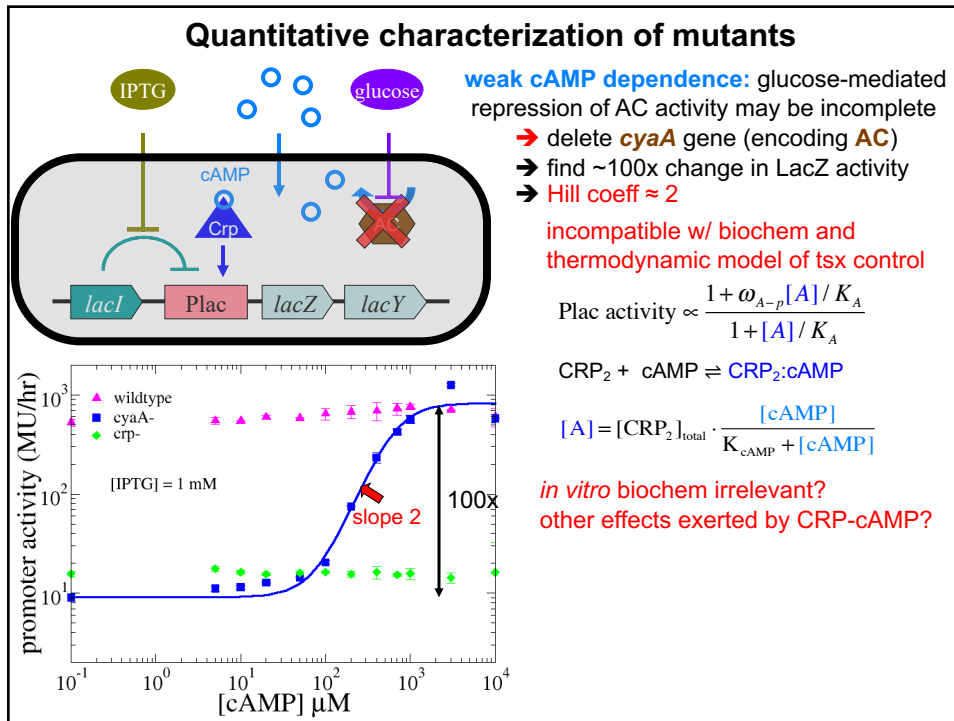
inconsistent with behavior of mutants:

$\Delta lacI$: > 1000x; Δcrp > 50x

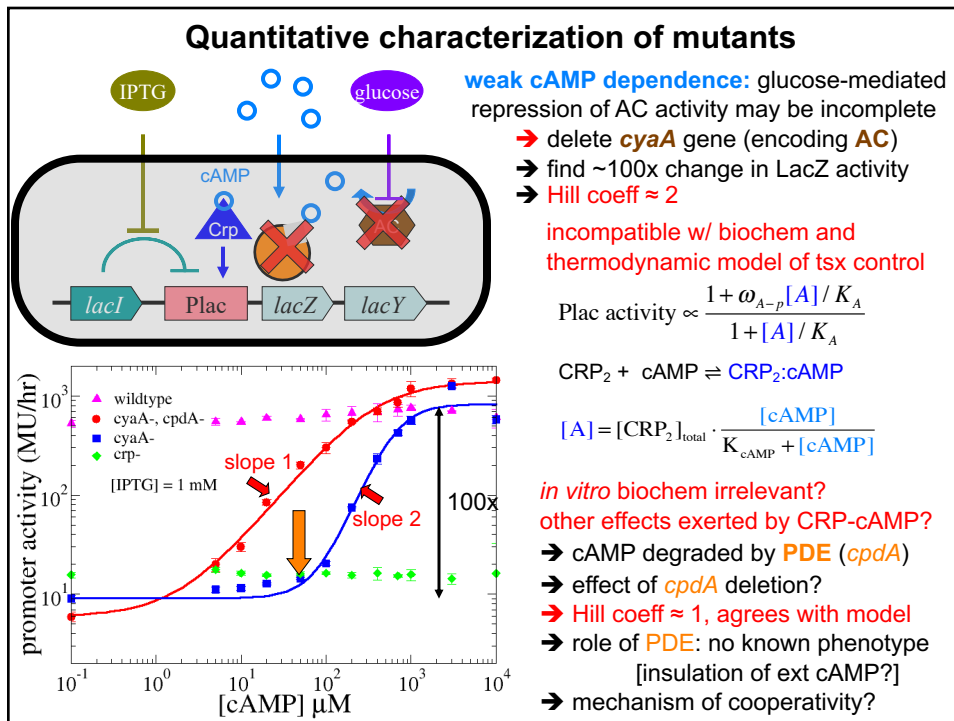
→ possible problems: complex links between extracellular and intracellular inducer conc.

theory

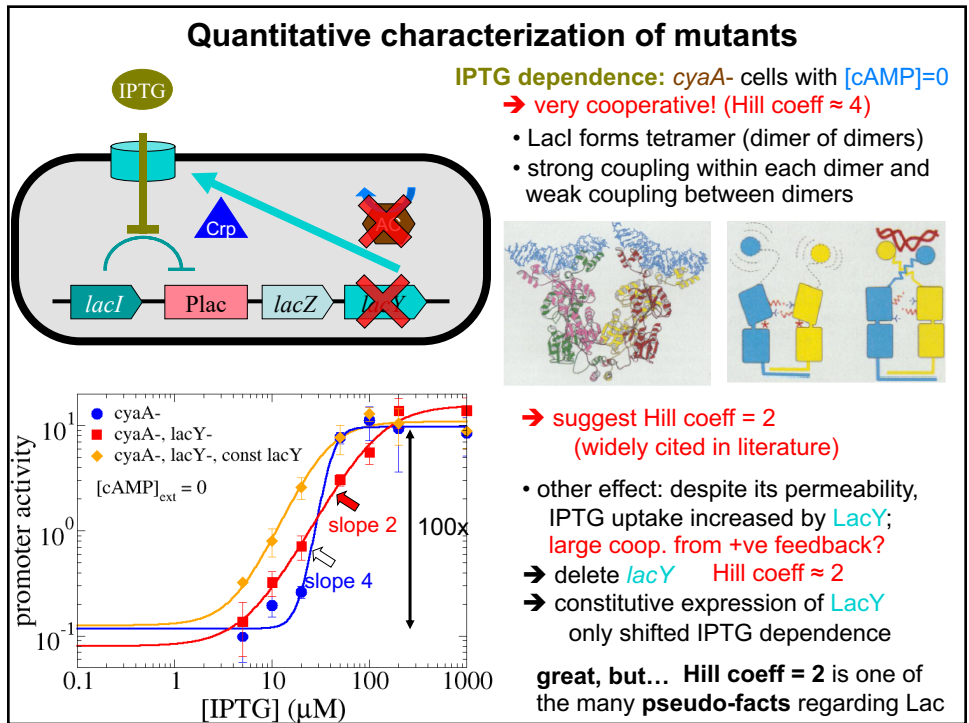
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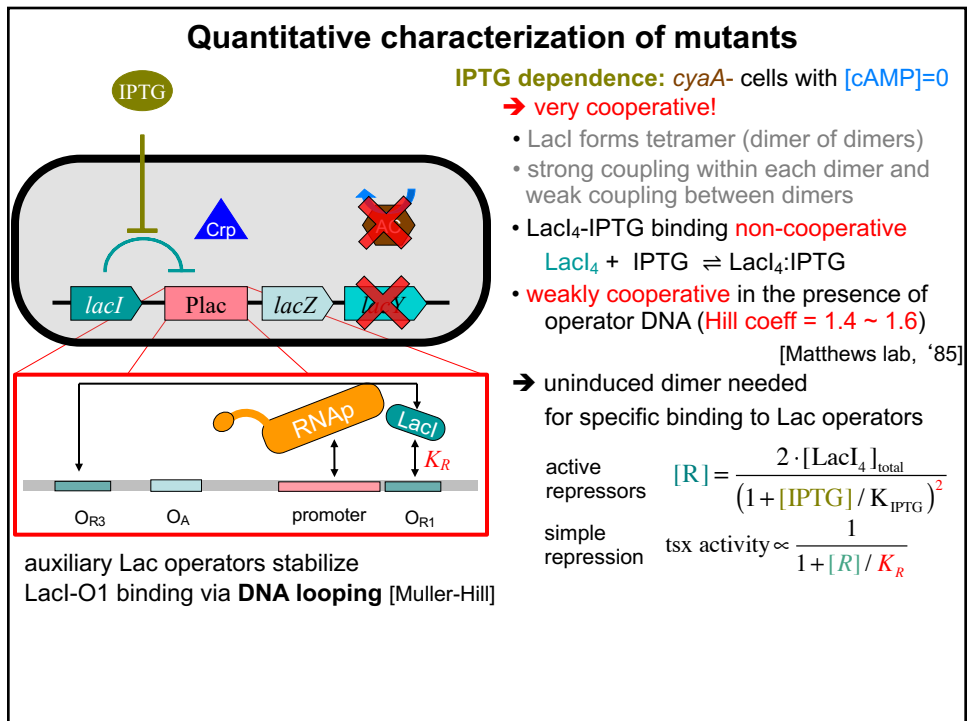
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Quantitative characterization of mutants

IPTG

Crp

Plac

lacI

lacZ

RNAP

O_{R3} O_A promoter O_{R1}

auxiliary Lac operators stabilize
LacI-O1 binding via **DNA looping** [Muller-Hill]

→ increase fold-repression
from $f = 2[\text{LacI}_4]/K_R$ to $f \cdot (1 + \mathcal{L}_0)$
but value of \mathcal{L}_0 not known independently

IPTG dependence: *cyaA*- cells with $[\text{cAMP}] = 0$
→ very cooperative!

- LacI forms tetramer (dimer of dimers)
- strong coupling within each dimer and weak coupling between dimers
- LacI₄-IPTG binding **non-cooperative**
 $\text{LacI}_4 + \text{IPTG} \rightleftharpoons \text{LacI}_4:\text{IPTG}$
- **weakly cooperative** in the presence of operator DNA (Hill coeff = 1.4 ~ 1.6)
[Matthews lab, '85]

→ uninduced dimer needed
for specific binding to Lac operators

active repressors $[\text{R}] = \frac{2 \cdot [\text{LacI}_4]_{\text{total}}}{(1 + [\text{IPTG}] / K_{\text{IPTG}})^2}$

simple repression $\text{tsx activity} \propto \frac{1}{1 + [\text{R}] / K_R}$

- include DNA looping in model

$$[\text{R}] \rightarrow [\text{R}] + \frac{\mathcal{L}_0 \cdot [\text{LacI}_4]_{\text{total}}}{(1 + [\text{IPTG}] / K_{\text{IPTG}})^4}$$

\mathcal{L}_0 : local increase of [LacI] due to looping

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Quantitative characterization of mutants

IPTG

cAMP

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lacI

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but value of \mathcal{L}_0 not known independently

looping model w/ $\mathcal{L}_0 \approx 12, 2[\text{LacI}_4]/K_R = 20$

promoter activity (MU/hr)

[IPTG] μM

- [cAMP] = 1 mM
- [cAMP] = 100 μM
- [cAMP] = 10 μM
- [cAMP] = 0

→ single parameter \mathcal{L}_0 fits both fold-repression and slope

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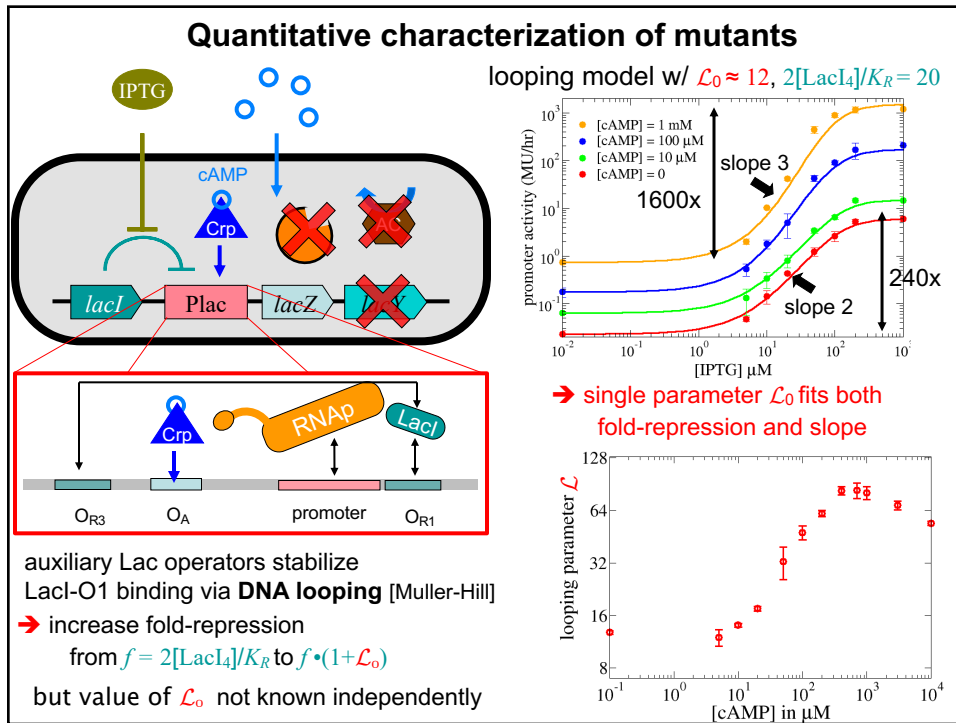
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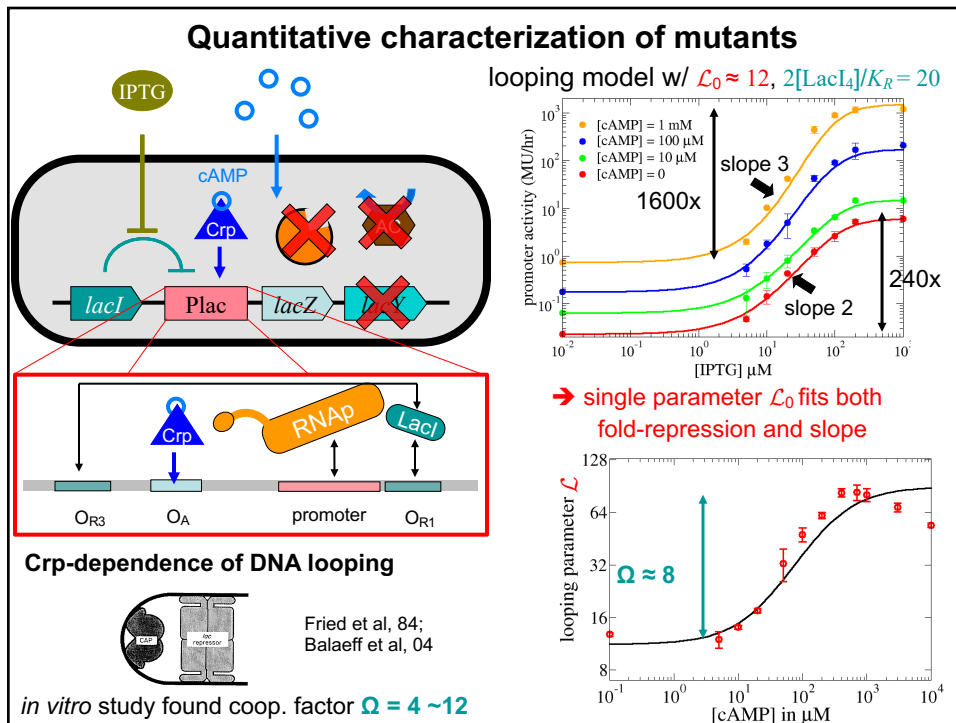
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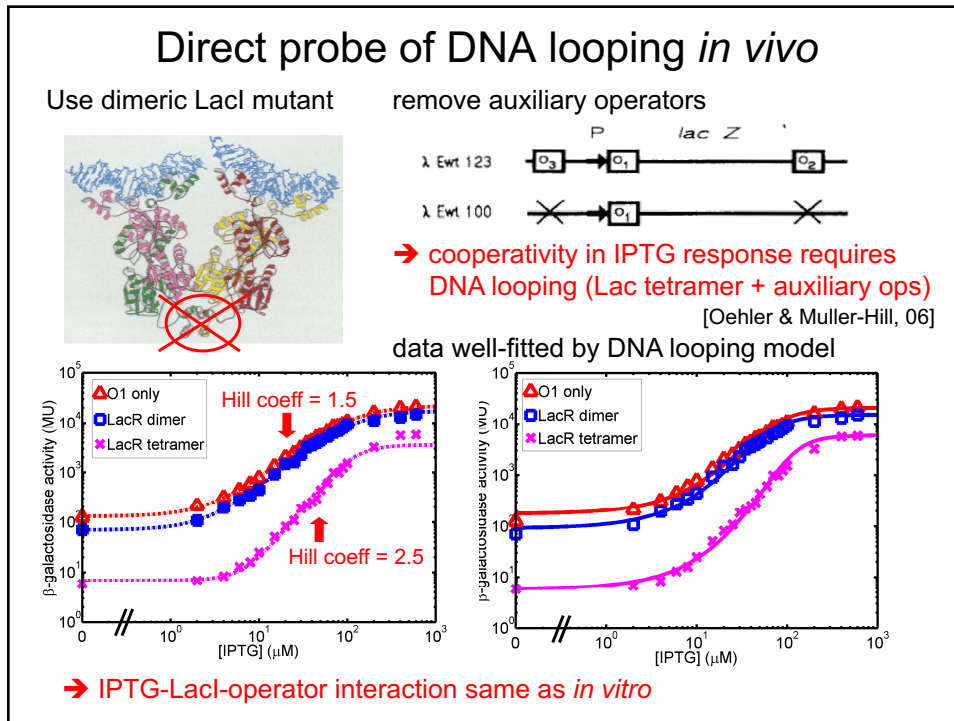
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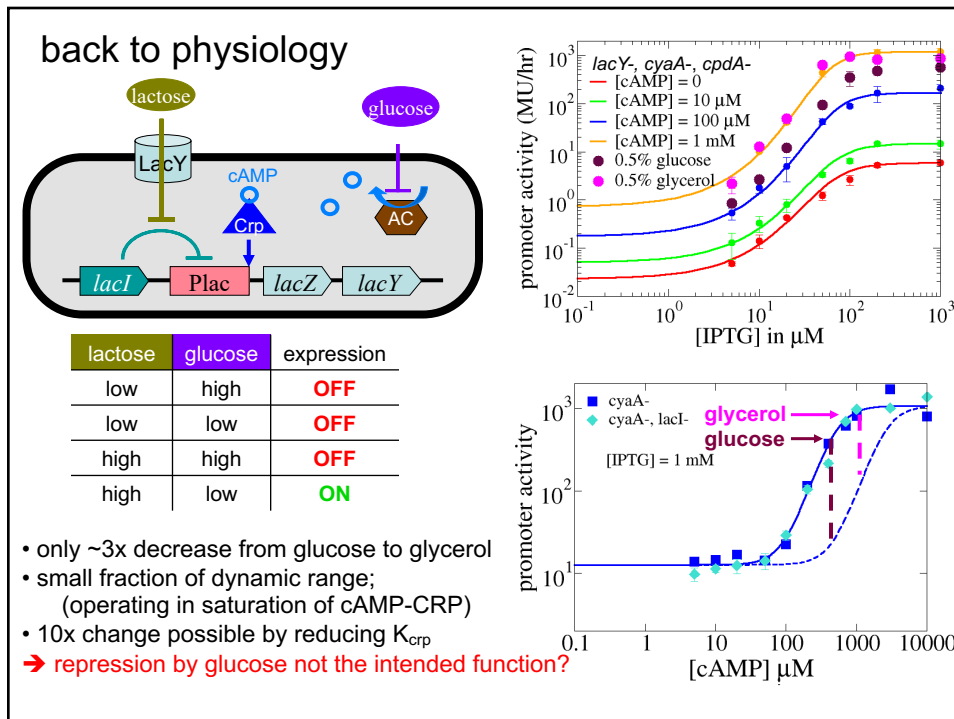
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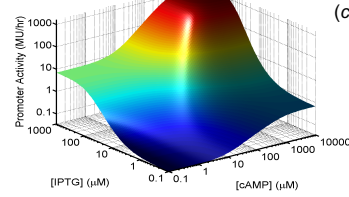
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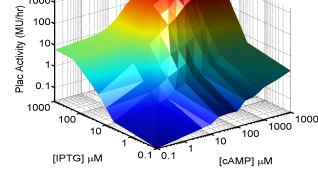
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Summary

theory



E. coli MG1655
(*cyaA*-, *cpdA*-, *lacY*-)



- **main findings for the *lac* promoter:**
 - Crp enhances DNA looping
 - abrupt IPTG response despite non-cooperative LacI-IPTG interaction;
 - **suggests physiological role of Crp-cAMP as enhancer of repression**
 - mechanism of Crp-LacI interaction?
 - coop cAMP response due to PDE; physiological function? mechanism?
- **general lessons for quantitative systems biology:**
 - hidden interaction and pseudo-facts abound even for the “best studied” system
 - quantitative description of *in vivo* biology is possible
 - need **solid, qualitative** knowledge of the components (e.g., Hill coeff)
(*in vitro* results surprisingly robust in this regard)
 - **(semi) quantitative** characterization generates spectrum of phenotypes
 - provides clues for identifying unknown components and mechanisms
 - provides **phenomenological description** of Plac for high-level studies